

# Discrete Adversarial Attacks and Submodular Optimization with Applications to Text Classification

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Joint work with

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## 1 Introduction to Adversarial Examples

## 2 General Framework

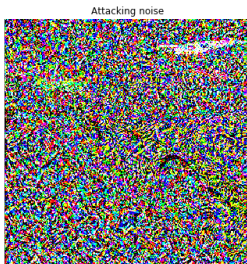
- Mathematical formulation
- Theoretical Findings

## 3 Our methods and Experiments

# What is Adversarial Examples?



sports car



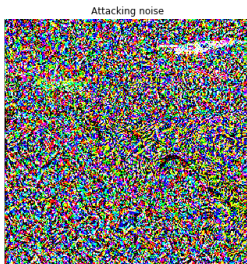
toaster

[1] Blog post by Emil Mikhailov and Roman Trusov: *How Adversarial Attacks Work*

# What is Adversarial Examples?



sports car



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- instances with **small, intentional** feature perturbations to make models predict incorrectly

[1] Blog post by Emil Mikhailov and Roman Trusov: *How Adversarial Attacks Work*

# Adversarial Examples for Discrete Data

Task: Sentiment Analysis.

Classifier: LSTM.

Original prediction: **100% Positive.**

I suppose I should write a review here since my little Noodle-oo is currently serving as their spokes dog in the photos. We both love Scooby Do's. (... 135 unchanged words omitted ...) The pricing is also cheaper than some of the big name conglomerates out there. I'm talking to you Petsmart! I've taken my other pup to Smelly Dog before, but unless I need dog sitting play time after the cut, I'll go with Scooby's. They genuinely seem to like my little Noodle monster.

# Adversarial Examples for Discrete Data

Task: Sentiment Analysis.

Classifier: LSTM.

ADV prediction: **100% Negative.**

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# Adversarial Examples for Discrete Data

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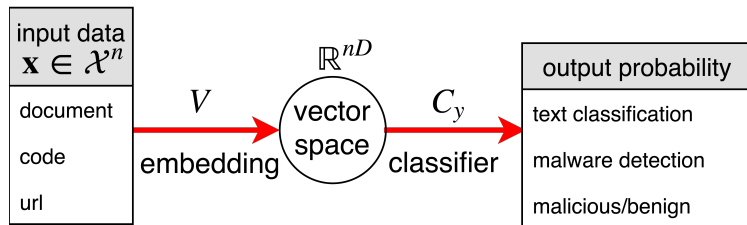
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- **small** feature perturbations
- A human should not be able to detect if the text has been manipulated.

- General framework of generating adversarial examples with discrete data:





# Candidate Generation

- small feature perturbations

# Candidate Generation

- **small feature perturbations**
- Pick up word/sentence candidate set by semantic and syntactic similarity.

1. select candidates by semantic distance

2. filter by syntactic distance

I	like	to	eat	lunch	in	this	cafe.
<del>we</del>	<del>likes</del>		have	dinner		the	restaurant
<del>me</del>	love		<del>eats</del>	breakfast		that	cafeteria
<del>my</del>	adore		<del>bite</del>	brunch		<del>these</del>	eatory

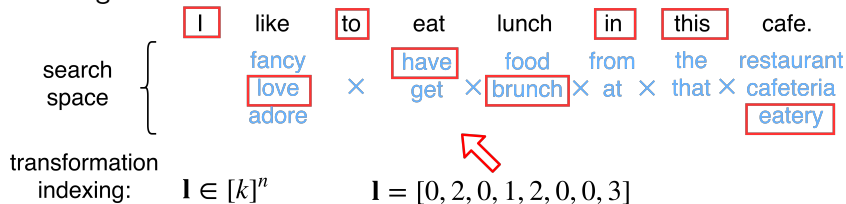
[1] V. Kuleshov, S. Thakoor, T. Lau, and S. Ermon, "Adversarial examples for natural language classification problems." 2018

# Attacking Procedure

- to make models predict incorrectly

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- to **make models predict incorrectly**
- Find a good combination from the candidate sets:



# A General Formulation

- We consider a target attack by selecting from possible candidates

## Problem 1 (target attack)

x: input document

x

# A General Formulation

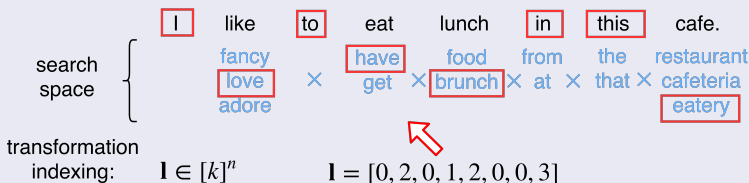
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## Problem 1 (target attack)

$x$ : input document

$T_I$ : word paraphrasing indexed by  $I$

$T_I(x)$



# A General Formulation

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$V$ : word2vec/bag of word embedding

$$V(T_I(x))$$

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## Problem 1 (target attack)

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$C$ : classifier that outputs target label's probability

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Find the best transformation labeled by  $I$ , with at most  $m$  word replacements

$$I^* = \underset{I \in [k]^n, \|I\|_0 \leq m}{\operatorname{argmax}} C(V(T_I(x))).$$

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Find the best transformation labeled by  $I$ , with at most  $m$  word replacements

$$I^* = \operatorname{argmax}_{I \in [k]^n, \|I\|_0 \leq m} C(V(T_I(x))).$$

Or equivalently

$$S^* = \operatorname{argmax}_{|S| \leq m} f(S), \quad (1)$$

$f$ : a set function,  $f(S) = \max_{\operatorname{supp}(I) \subset S} C(V(T_I(x)))$

$S$ : support of  $I$ , indicating the words to be changed

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# Hardness: NP hardness

Problem is computationally intractable:

## Lemma 1

For a general classifier  $C$ , problem 1 is NP-hard. Even for a convex  $C$ , problem 1 can be polynomially reduced from subset sum and hence is NP-hard.

# Theoretical support for greedy methods

## Fact: Submodular Optimization

The problem of maximizing a monotone submodular function subject to a cardinality constraint admits a  $1 - 1/e$  approximation with greedy method.

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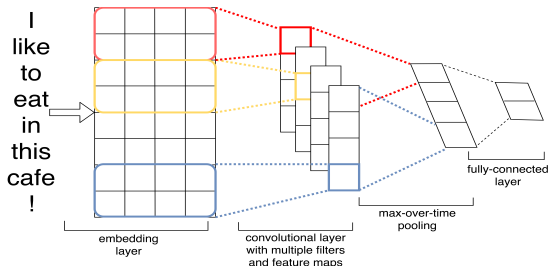
## Fact: Submodular Optimization

The problem of maximizing a monotone submodular function subject to a cardinality constraint admits a  $1 - 1/e$  approximation with greedy method.

- Our target function  $f(S)$  is monotone non-decreasing
- Do some non-trivial neural networks yield submodular functions?

# Neural Networks with submodular property for discrete set of attacks

## Simplified W-CNN [1]



## Theorem 1

For W-CNN classifier with no softmax layer, no overlaps between each window, and nonnegative weights in the last layer,  $f^{\text{WCNN}}(S)$  is submodular.

[1] Yoon Kim, "Convolutional Neural Networks for Sentence Classification", EMNLP 2014.



# Neural Networks with submodular property for discrete set of attacks

## one-hidden-node recurrent neural network

$$h_t = \phi(\mathbf{w}h_{t-1} + \mathbf{m}^\top \mathbf{v}_{t-1} + b) \quad (2)$$

### Theorem 2

For RNN with  $T$  time steps and single hidden nodes as in (2), if the activation is a non-decreasing concave function, then  $f^{\text{RNN}}(S)$  is submodular.

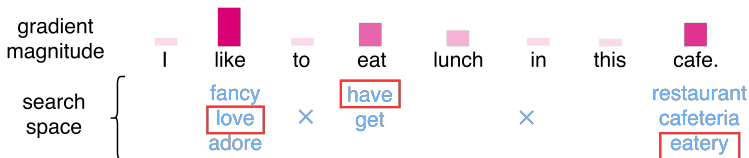
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# Methodology: Gradient-guided Greedy Method

Intuition: one replacement a time,  $\implies$  greedy method is slow

With the gradient information, we

- pick up  $M$  most important words to replace, (e.g. {like, eat, cafe})
- greedy search over the replacements for these  $M$  words



- Replace  $M$  words at a time.

# Comparisons with prior work

- [1] V. Kuleshov, S. Thakoor, T. Lau, and S. Ermon, “Adversarial examples for natural language classification problems.” 2018. (Objective-guided greedy)
- [2] Z. Gong, W. Wang, B. Li, D. Song, and W.-S. Ku, “Adversarial texts with gradient methods.” 2018. (Gradient method)

# Comparisons with prior work

**Table:** Comparisons with [1] and [2], on WCNN classifier with 5% dropout, with up to 20% word replacements. (ASR denotes attack success rate)

Method	objective-guided greedy [1]	gradient [2]	ours
Fake News Detection	<u>ASR:</u> 28.4%	12.8%	<b>45.4%</b>
	<u>time (s):</u> 1.46	<b>0.21</b>	0.31

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Spam Filtering	<u>ASR:</u> 24.9%	3.4%	<b>45.3%</b>
	<u>time (s):</u> 0.33	<b>0.05</b>	0.09

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Yelp Review Evaluation	<u>ASR:</u> 45.0%	9.1%	<b>55.9%</b>
	<u>time (s):</u> 0.21	<b>0.03</b>	0.05

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5 people randomly evaluate 60 texts for each task.

Dataset	News	Trec07p	Yelp
Original	70.0%	80.0%	100.0%
Adversarial	50.0%	80.0%	100.0%

Table: Classification Accuracy.



# Human Evaluation

5 people randomly evaluate 60 texts for each task.

Dataset	News	Trec07p	Yelp
Original	70.0%	80.0%	100.0%
Adversarial	50.0%	80.0%	100.0%

Table: Classification Accuracy.

Dataset	News	Trec07p	Yelp
Original	$3.06 \pm 0.67$	$3.23 \pm 0.31$	$1.93 \pm 0.55$
Adversarial	$3.13 \pm 0.50$	$3.10 \pm 0.40$	$2.10 \pm 1.05$

Table: Quality of the text: On a scale of 1-5, how likely the text is human written.

- Theoretical part:
  - NP-hardness
  - Explore submodularity for some neural networks

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  - NP-hardness
  - Explore submodularity for some neural networks
- Experimental part:
  - Practical method: gradient-guided greedy method
  - ★ We use sentence paraphrasing to expand the space of attacks
    - Experiments verified on three different tasks
    - Human Evaluation
  - ★ Adversarial training

Thank you!

# Methodology: Joint sentence and word paraphrasing attack

- Pick up sentence candidate set from semantic similarity.
- Greedily conduct sentence level paraphrasing attacks.

I've always run jigdo-lite against my own mirror. It provides two things: 1) Proves ~~to~~ **you are able to** build the ISOs from what I have mirrored locally. 2) Doesn't waste additional bandwidth. ...

- Pick up word candidate set from semantic and syntactic similarity.
- Greedily conduct word level paraphrasing attacks

I've always run jigdo-lite against my own mirror. It ~~provides~~ **offers** two things: 1) Proves ~~to~~ **you are able to** build the ISOs from what I have mirrored locally. 2) Doesn't waste additional bandwidth. As long as the checksums match what is provided from the official ISO image masters site, I don't see what the difference would be. Anyone else do this? :-)^ \_ ^

# Experiment: Joint sentence and word paraphrasing attack

**Table:** Experiments on Word-level CNN with 5% dropout. [1] allows 50% word replacement while we only allow 20% word paraphrasing and 20% sentence paraphrasing.

Accuracy	Origin	ADV (ours)	ADV [1]
News	93.1%	35.4%	71.0%
Trec07p	99.1%	48.6%	64.5%
Yelp	93.6%	23.1%	39.0%

[1] V. Kuleshov, S. Thakoor, T. Lau, and S. Ermon, “Adversarial examples for natural language classification problems.”

# Experiments: Adversarial Training

Table: Performance of adversarial training.

Dataset	News	Trec07p	Yelp
Test (before)	93.1%	99.1%	93.6%
Test (after)	93.8%	99.2%	94.9%
ADV (before)	35.4%	48.6%	23.1%
ADV (after)	40.0%	54.2%	44.4%